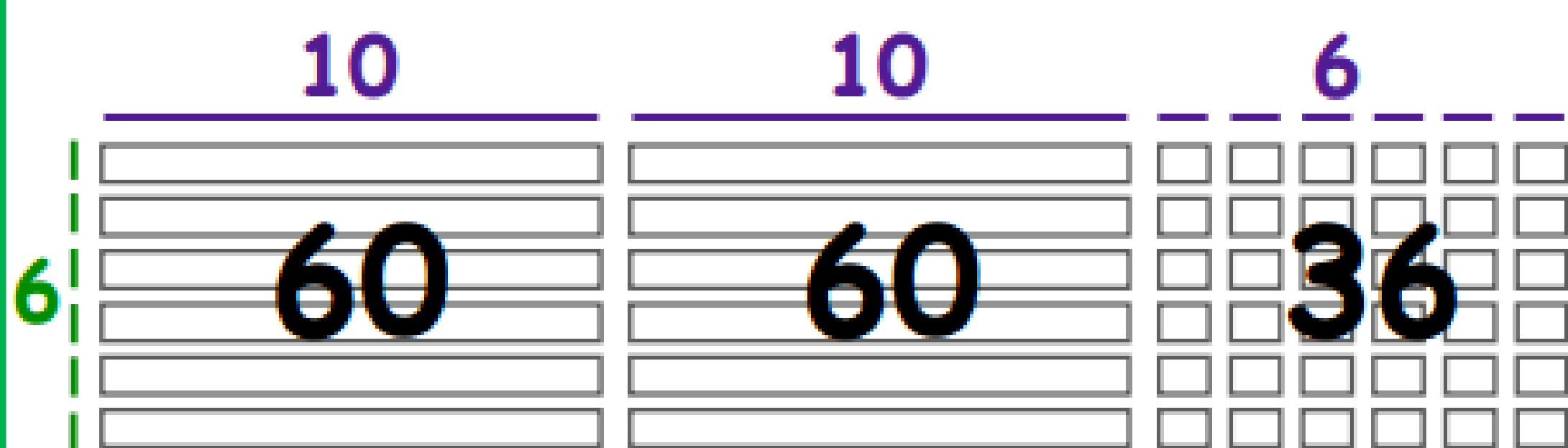


Multiplication Strategies

Build an Array with Base Ten Pieces

$$26 \times 6$$

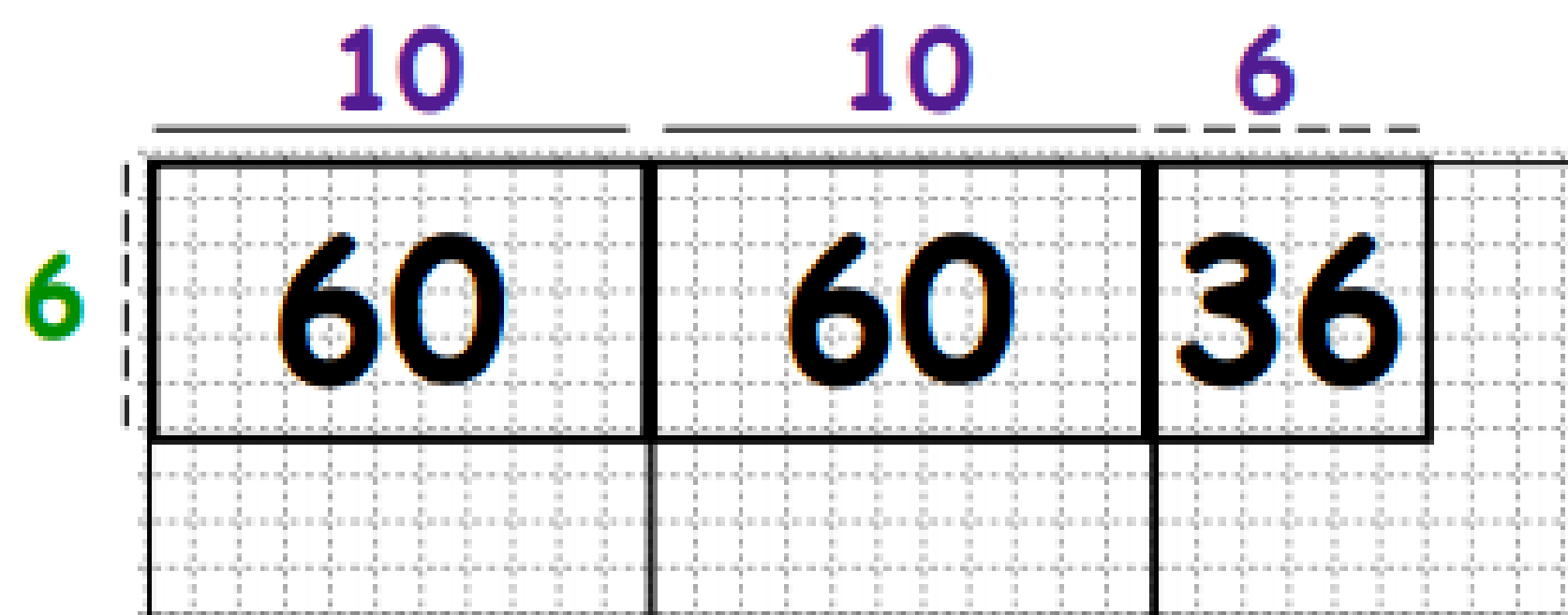


$$60 + 60 + 36 = 156$$

Build an Array with Grid Paper

Grid Paper

$$26 \times 6$$



$$60 + 60 + 36 = 156$$

Distributive Property (Break Apart Numbers)

$$3 \times 18 = ?$$

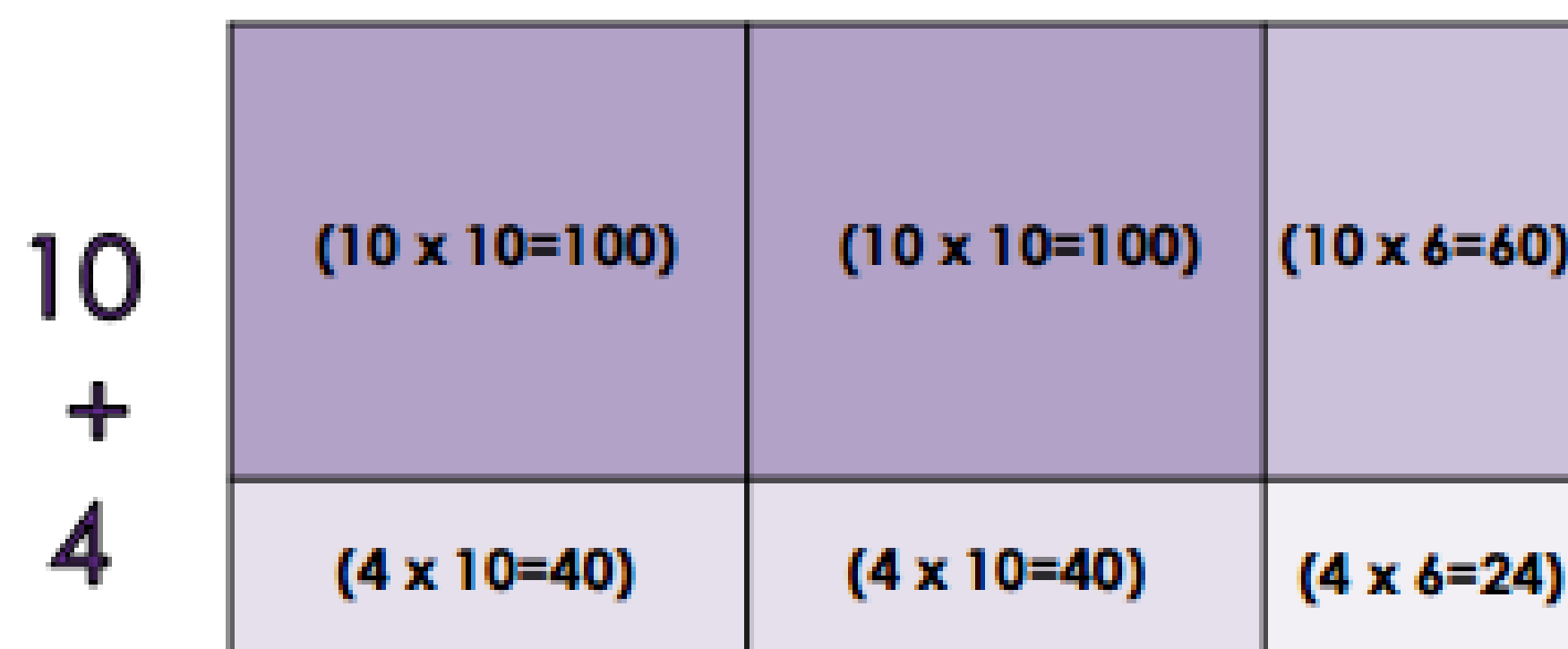
$$(3 \times 10) + (3 \times 8)$$

$$30 + 24 = 54$$

Area Model

$$14 \times 26 = ?$$

$$10 + 10 + 6$$



$$100 + 100 + 60 + 40 + 40 + 24 = 364$$

Partial Products

$$42 \times 53 = ?$$

$$\begin{array}{r} 42 \\ \times 53 \\ \hline \end{array}$$

$$50 \times 40 = 2000$$

$$50 \times 2 = 100$$

$$3 \times 40 = 120$$

$$3 \times 2 = 6$$

$$2226$$

Doubling & Halving

Multiply one number by 2. Divide the other number by 2. Keep going until you reach friendlier numbers.

$$\begin{array}{l} \div 2 \left\{ \begin{array}{l} 8 \times 25 \\ 4 \times 50 \end{array} \right. \times 2 \\ \div 2 \left\{ \begin{array}{l} 4 \times 50 \\ 2 \times 100 \end{array} \right. \times 2 \end{array}$$

$$2 \times 100 = 200$$

Division Strategies

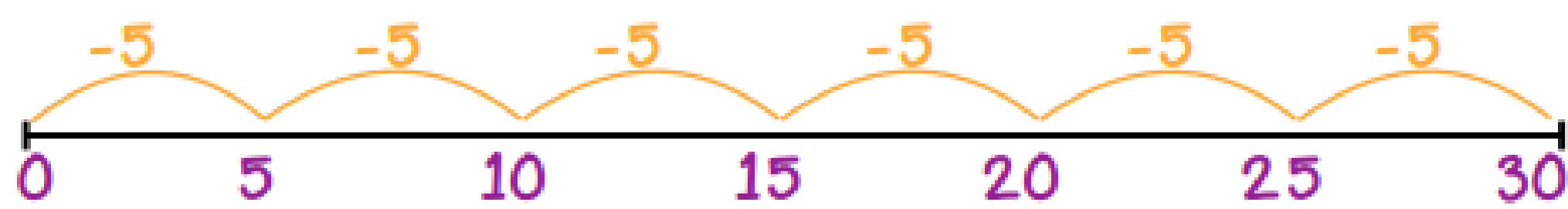
Repeated Subtraction

Think of the divisor as groups and remove the groups from the whole until there are zero.

$$30 \div 5$$

$$30 - 5 - 5 - 5 - 5 - 5 - 5 = 0$$

5 is subtracted 6 times



$$30 \div 5 = 6$$

Multiplying Up

Start with the divisor and then multiply up to the dividend using facts you already know.

$$384 \div 16$$

$$10 \times 16 = 160$$

$$10 \times 16 = 160$$

$$2 \times 16 = 32$$

$$2 \times 16 = 32$$

$$10 + 10 + 2 + 2 = 24$$

384

320

64

Partial Quotients

Work your way toward the quotient by using friendly multipliers such as tens, fives, and twos.

$\begin{array}{r} 6 \overline{) 962} \\ \underline{600} \\ 362 \\ \underline{120} \\ 242 \\ \underline{240} \\ 2 \end{array}$	$\begin{array}{l} \times 100 \\ \times 20 \\ \times 40 \\ \hline 160 \text{ R } 2 \end{array}$	$\begin{array}{r} 6 \overline{) 962} \\ \underline{600} \\ 362 \\ \underline{180} \\ 182 \\ \underline{180} \\ 2 \end{array}$	$\begin{array}{l} \times 100 \\ \times 30 \\ \times 30 \\ \hline 160 \text{ R } 2 \end{array}$
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Proportional Reasoning

Divide both numbers by the same amount to create an easier problem.

$$\begin{array}{c} \div 2 \left\{ \begin{array}{l} 384 \div 16 \\ \downarrow \\ 192 \div 8 \\ \downarrow \\ 96 \div 4 \\ \downarrow \\ 48 \div 2 \end{array} \right. \div 2 \\ \div 2 \left\{ \begin{array}{l} 192 \div 8 \\ \downarrow \\ 96 \div 4 \\ \downarrow \\ 48 \div 2 \end{array} \right. \div 2 \\ \div 2 \left\{ \begin{array}{l} 96 \div 4 \\ \downarrow \\ 48 \div 2 \end{array} \right. \div 2 \\ \div 2 \left\{ \begin{array}{l} 48 \div 2 \end{array} \right. \div 2 \\ \hline = 24 \end{array}$$

Addition Strategies

Decomposing Strategy

$$345 + 623 = \boxed{?}$$

$$345 = 300 + 40 + 5$$

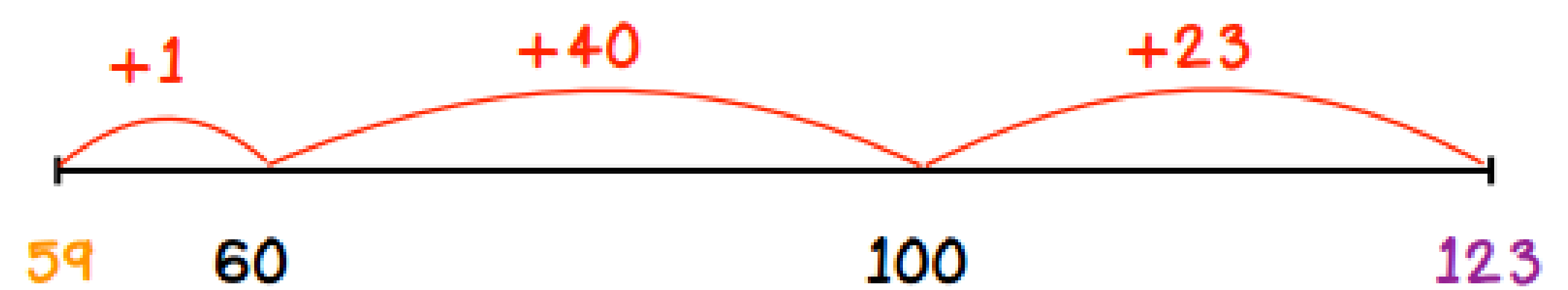
$$623 = 600 + 20 + 3$$

$$900 + 60 + 8 = \boxed{968}$$

Adding Up

Start on a number line with one of the numbers being added and add the other number in easy-to-work-with chunks.

$$59 + 64 =$$



$$59 + 1 + 40 + 23 = \boxed{123}$$

Branching Strategy

$$88 + 36 = \boxed{?}$$

$$\begin{array}{cc} 88 & + & 36 \\ \swarrow & & \searrow \\ 80 + 8 & & 30 + 6 \end{array}$$

$$110 + 14 = \boxed{124}$$

Friendly Numbers

Adjust the numbers so they are easier to add.

$$\begin{array}{r} 116 + 118 \\ + \quad 2 \\ \hline \end{array}$$

$$116 + 120 = 236$$

Don't forget to re-adjust for the 2 you added!

$$236 - 2 = \boxed{234}$$

Partial Sums Strategy

$$64 + 27 = ?$$

$$\begin{array}{r} 64 \\ +27 \\ \hline \end{array}$$

$$\begin{array}{r} 64 \\ +27 \\ \hline \end{array}$$

$$60 + 20 = 80 \quad \text{- or -} \quad 4 + 7 = 11$$

$$4 + 7 = +11 \quad \quad \quad 60 + 20 = +80$$

$\boxed{91}$

$\boxed{91}$

Compensation

Take a specific amount away from one number and add that exact amount to the other to make friendlier numbers.

$$\begin{array}{r} 116 + 118 \\ - 2 \quad + 2 \\ \hline \end{array}$$

$$114 + 120 = \boxed{234}$$

Subtraction Strategies

Decomposing Strategy

$$647 - 234 = \boxed{?}$$

$$647 = 600 + 40 + 7$$

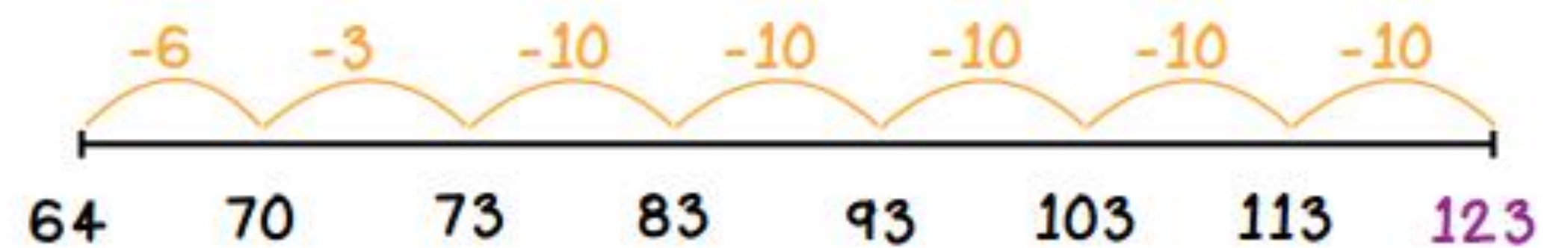
$$-234 = -200 + 30 + 4$$

$$400 + 10 + 3 = \mathbf{413}$$

Removal / Counting Back

Start with the whole (the minuend), and then remove parts in easy-to-use chunks to get to the number being subtracted (the subtrahend).

$$\text{minuend} \rightarrow 123 - 59 \leftarrow \text{subtrahend}$$

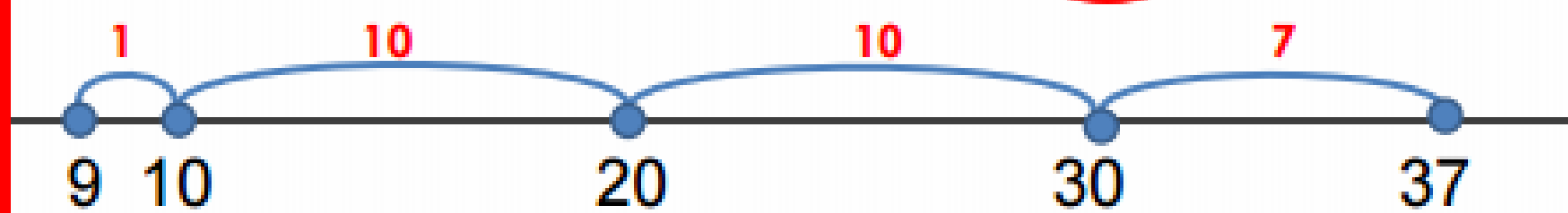


$$123 - 10 - 10 - 10 - 10 - 10 - 3 - 6 = \mathbf{64}$$

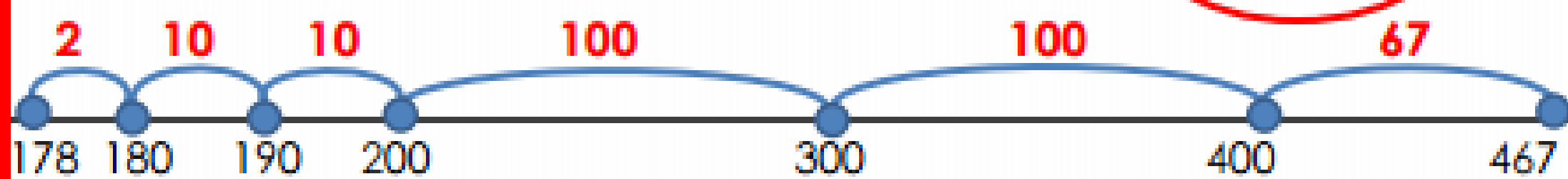
59

Open Number Line

$$37 - 9 = \mathbf{28}$$



$$467 - 178 = \mathbf{289}$$



Adjust One Number

Adjust one number to make the problem easier to subtract.

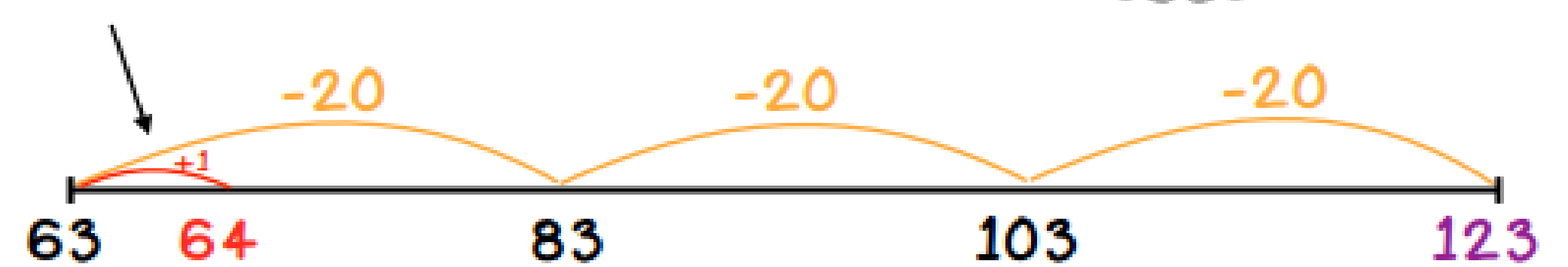
$$123 - 59$$

$$+ 1$$

You made the difference bigger by adding 1. Remember to re-adjust at the end!

$$123 - 60 = 63$$

$$\rightarrow 63 + 1 = \mathbf{64}$$



Zero Zapper

$$300 - 138 = \boxed{?}$$

$$300 - 1 = 299$$

$$- 138 - 1 = -137$$

$$\mathbf{162}$$

Keeping a Constant Difference

Add or subtract the same amount from both numbers to make the problem friendlier. This keeps the difference constant and does not change the answer.

$$123 - 59$$

$$+ 1 \quad + 1$$

$$124 - 60 = \mathbf{64}$$

